

Visit

[FreeTestPaper.com](http://FreeTestPaper.com)

for more papers



BEATTY SECONDARY SCHOOL  
MID-YEAR EXAMINATION 2015

SUBJECT : Mathematics

LEVEL : Secondary 2 Express

PAPER : 1

DURATION : 1 hour 15 minutes

SETTER : Mr Anthony Goh

DATE : 15 May 2015

CLASS :	NAME :	REG NO :
---------	--------	----------

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number in the spaces on the top of this page.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** questions.

If working is needed for any question, it must be shown with the answer.

Omission of essential working will result in loss of marks.

Calculators should be used where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142, unless the question requires the answer in terms of  $\pi$ .

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is 50.

For Examiner's Use
50

This paper consists of 11 printed pages (including this cover page)

[Turn over

Answer all questions.

1 (a) Expand and simplify  $(a+3)(2a-3)$ .

(b) Simplify  $(-4x^2)(4x)^2$ .

Answer (a) ..... [1]

(b) ..... [2]

2 Solve each of the following equations.

(a)  $(2p+3)(p-5) = 0$ ,

(b)  $x^2 = 7x$ .

Answer (a)  $p =$  ..... [1]

(b)  $x =$  ..... [2]

3 Factorise **completely** each of the following expressions.

(a)  $5w^2 - 23w + 12$

(b)  $50c^2 - 98d^2$

Answer (a) ..... [1]

(b) ..... [2]

4 Solve  $\frac{2}{5z-1} = -\frac{3}{4}$ .

Answer  $z =$  ..... [2]

5 A map has a scale of 1:400 000.

- (a) Given that the actual distance between two locations  $A$  and  $B$  is 14 km, find the distance, in cm, between  $A$  and  $B$  on the map.
- (b) Given that the area of a garden on the map is  $1.5 \text{ cm}^2$ , calculate its actual area in  $\text{km}^2$ .

*Answer (a)* ..... cm [2]

*(b)* .....  $\text{km}^2$  [2]

6 The kinetic energy,  $E$  joules, of a particular object is directly proportional to the square of its velocity  $v$  m/s. Given that  $E = 75$  joules when  $v = 2.5$  m/s, find

- (a) the equation connecting  $E$  and  $v$ ,  
 (b) the value of  $v$ , in m/s, when  $E = 432$  joules.

Answer (a) ..... [2]

(b)  $v =$  ..... m/s [2]

7 (a) Factorize  $x^2 - 9$ .

(b) Hence, find 2 factors of 2491, other than 1 and 2491.

Answer (a) ..... [1]

(b) ..... , ..... [2]

8 4 workers can complete an assignment in 15 days. Assuming all the workers work at the same rate, find

- (a) the number of days taken by 3 workers to complete the assignment,
- (b) the number of additional workers needed if the assignment is to be completed in 10 days.

*Answer (a)* ..... days [2]

*(b)* ..... additional workers [2]

9 (a) Express  $\frac{1}{2x+1} + \frac{2}{3x-2}$  as a single fraction in its simplest form.

(b) Simplify  $\frac{a^3b^2c^3}{24c^4} \div \frac{a^3b}{8c}$ .

Answer (a) ..... [2]

(b) ..... [2]

4

[Turn Over

10 Simplify each of the following expressions.

(a)  $\frac{2n^2 + 3n}{16n + 24}$ ,

(b)  $\frac{e^4 f^2 - e^3 f^3}{e^2 f^4 - e^3 f^3}$ .

Answer (a) ..... [2]

(b) ..... [2]

11 Solve  $(x + 3)(x - 5) = 20$ .

Answer  $x =$  ..... [3]

12 Given that  $p = \sqrt{\frac{2-q}{3+q}}$ ,

- (a) find the value of  $p$  when  $q = -\frac{5}{2}$ ,
- (b) express  $q$  in terms of  $p$ .

Answer (a)  $p = \dots\dots\dots$  [2]

(b)  $q = \dots\dots\dots$  [3]

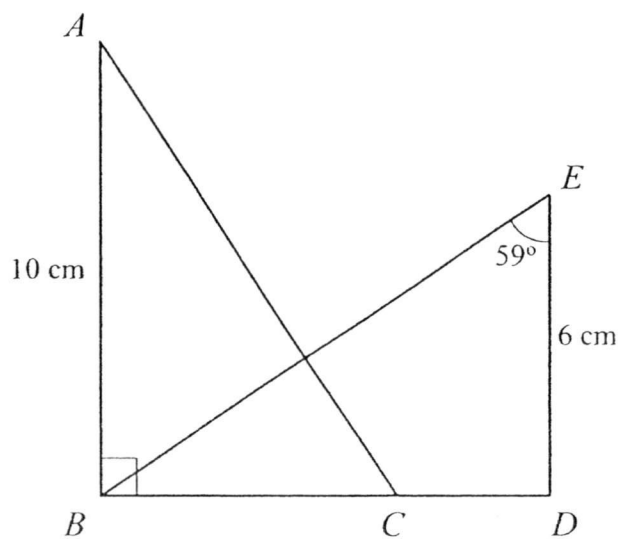
5

[Turn Over

- 13 In the figure below,  $\triangle ABC$  is congruent to  $\triangle BDE$ ,  
 $\angle ABC = 90^\circ$ ,  $\angle BED = 50^\circ$ ,  $AB = 10$  cm and  $DE = 6$  cm.

Find

- (a)  $\angle BAC$ ,  
 (b) the length of  $CD$ .



Answer (a)  $\angle BAC = \dots\dots\dots$  [2]

(b)  $CD = \dots\dots\dots$  cm [2]

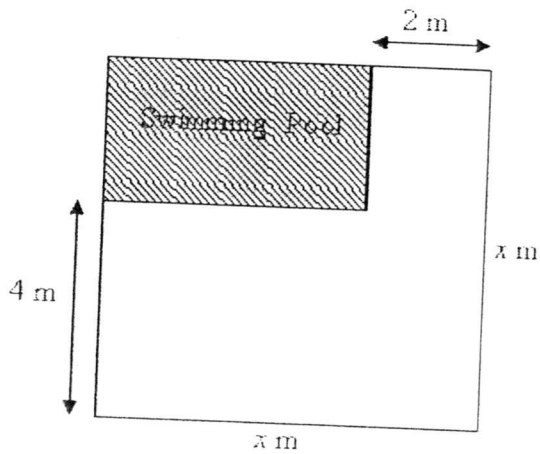
14 Ahmad decided to build a swimming pool in his house on a square plot of land of side  $x$  metres.

(a) Write down an expression, in terms of  $x$ , for the area of the swimming pool.

(b) The area of the swimming pool was found to be  $80 \text{ m}^2$ .

Show that  $x^2 - 6x - 72 = 0$ .

(c) Hence, find the value of  $x$ .



Answer (a) Area = .....  $\text{m}^2$  [1]

(b) Answer to be shown above [1]

(c)  $x =$  ..... [2]

## ANSWER KEY

1. a) $2a^2 + 3a - 9$ b) $-64x^4$	2. a) $p = -\frac{3}{2}$ or 5 b) $x = 0$ or 7	3. a) $(5w-3)(w-4)$ b) $2(5c+7d)(5c-7d)$
4. $z = -\frac{1}{3}$	5. a) 3.5 cm b) $24 \text{ km}^2$	6. a) $E = 12v^2$ b) $v = \pm 6$
7. a) $(x+3)(x-3)$ b) 47 and 53	8. a) 20 days b) 2 additional workers	9. a) $\frac{7x}{(2x+1)(3x-2)}$ b) $\frac{b}{3}$
10. a) $\frac{n}{8}$ b) $-\frac{e}{f}$	11. $x = 7$ or $-5$	12. a) 3 b) $\frac{2-3p^2}{p^2+1}$
13. a) $31^0$ b) 4 cm	14. a) $(x-2)(x-4)$ c) 12	



BEATTY SECONDARY SCHOOL  
MID-YEAR EXAMINATION 2015

SUBJECT : Mathematics

LEVEL : Secondary 2 Express

PAPER : 1

DURATION : 1 hour 15 minutes

SETTER : Mr Anthony Goh

DATE : 15 May 2015

CLASS :	NAME :	REG NO :
---------	--------	----------

Marking  
Scheme

READ THESE INSTRUCTIONS FIRST

Write your name, class and index number in the spaces on the top of this page.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** questions.

If working is needed for any question, it must be shown with the answer.

Omission of essential working will result in loss of marks.

Calculators should be used where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142, unless the question requires the answer in terms of  $\pi$ .

The number of marks is given in brackets [ ] at the end of each question or part question.

The total number of marks for this paper is **50**.

For Examiner's Use
50

This paper consists of 11 printed pages (including this cover page)

7

[Turn over

## Answer all questions.

1 (a) Expand and simplify  $(a+3)(2a-3)$

(b) Simplify  $(-4x^2)(4x)^2$

$$\begin{aligned} \text{(a)} \quad (a+3)(2a-3) &= 2a^2 - 3a + 6a - 9 \\ &= 2a^2 + 3a - 9 \end{aligned} \quad [\text{B1}]$$

$$\begin{aligned} \text{(b)} \quad (-4x^2)(4x)^2 &= (-4x^2)(16x^2) \quad [\text{M1}] \\ &= -64x^4 \quad [\text{A1}] \end{aligned}$$

Answer (a) ..... [1]

(b) ..... [2]

2 Solve each of the following equations.

(a)  $(2p+3)(p-5) = 0$

(b)  $x^2 = 7x$

$$\begin{array}{l} (2p+3)(p-5) = 0 \\ \text{(a)} \quad 2p+3 = 0 \quad \text{OR} \quad p-5 = 0 \\ \quad \quad \quad p = -\frac{3}{2} \quad \quad \quad p = 5 \quad \quad \quad [\text{B1}] \end{array}$$

$$\begin{array}{l} x^2 = 7x \\ \text{(b)} \quad x^2 - 7x = 0 \\ \quad \quad x(x-7) = 0 \quad \quad \quad [\text{M1}] \\ \quad \quad x = 0 \quad \text{or} \quad 7 \quad \quad \quad [\text{A1}] \end{array}$$

Answer (a)  $p =$  ..... [1]

(b)  $x =$  ..... [2]

3 Factorise **completely** each of the following expressions.

(a)  $5w^2 - 23w + 12$

(b)  $50c^2 - 98d^2$

(a)  $5w^2 - 23w + 12 = (5w - 3)(w - 4)$  [B1]

(b)  $50c^2 - 98d^2 = 2(25c^2 - 49d^2)$  [M1]  
 $= 2(5c + 7d)(5c - 7d)$  [A1]

Answer (a) ..... [1]

(b) ..... [2]

4 Solve  $\frac{2}{5z-1} = -\frac{3}{4}$

$\frac{2}{5z-1} = -\frac{3}{4}$   
 $15z - 3 = -8$  [M1]

$15z = -5$

$z = -\frac{1}{3}$  [A1]

Answer  $z =$  ..... [2]

5 A map has a scale of 1:400 000.

- (a) Given that the distance between two locations  $A$  and  $B$  is 14 km, find the distance, in cm, between  $A$  and  $B$  on the map.
- (b) Given that the area of a garden on the map is  $1.5 \text{ cm}^2$ , calculate its actual area in  $\text{km}^2$ .

(a) Map scale = 1 cm : 400 000 cm  
 = 1 cm : 4 km  
 =  $\frac{1}{4}$  cm : 1 km

$$\text{Distance on map} = 14 \times \frac{1}{4} \quad \text{[M1]}$$

$$= 3.5 \text{ cm} \quad \text{[A1]}$$

(b) Map scale = 1 cm : 4 km  
 Area scale =  $1 \text{ cm}^2 : 16 \text{ km}^2$

$$\text{Actual area} = 1.5 \times 16 \quad \text{[M1]}$$

$$= 24 \text{ km}^2 \quad \text{[A1]}$$

Answer (a) ..... cm [2]

(b) .....  $\text{km}^2$  [2]

- 6 The kinetic energy,  $E$  joules, of a particular object is directly proportional to the square of its velocity  $v$  m/s. Given that  $E = 75$  joules when  $v = 2.5$  m/s, find
- (a) the equation connecting  $E$  and  $v$ ,
- (b) the value of  $v$ , in m/s, when  $E = 432$  joules.

$$E = kv^2$$

When  $E = 75$ ,  $v = 2.5$ ,

(a)  $75 = k(2.5)^2$  [M1]

$$k = 12$$

$$\therefore E = 12v^2$$
 [A1]

$$432 = 12v^2$$
 [M1]

(b)  $v^2 = 36$

$$v = 6$$
 [A1]

Accept  $v = -6$  as well, as it is not obvious to the students whether  $v$  can be positive or negative.

Answer (a) ..... [2]

(b)  $v =$  ..... m/s [2]

- 7 (a) Factorize  $x^2 - 9$ .
- (b) Hence, find 2 factors of 2491, other than 1 and 2491.

(a)  $x^2 - 9 = (x+3)(x-3)$  [B1]

$$2491 = 2500 - 9$$
 [M1]

$$= 50^2 - 3^2$$

(b)  $= (50-3)(50+3)$

$$= (47)(53)$$

$\therefore$  the other 2 factors are 47 and 53. [A1]

Answer (a) ..... [1]

(b) ..... , ..... [2]

8 4 workers can complete an assignment in 15 days. Assuming all the workers work at the same rate, find

- (a) the number of days taken by 3 workers to complete the assignment,  
 (b) the number of additional workers needed if the assignment is to be completed in 10 instead of 15 days.

(a)	Workers	Days	
	4	15	
	1	$15 \times 4 = 60$	[M1]
	3	$60 \div 3 = 20$	[A1]

(b)	Workers	Days	
	$3 \times 2 = 6$	$20 \div 2 = 10$	[M1]
	$\therefore (6-4) = 2$ extra workers are needed.		[A1]

Answer (a) ..... [2]

(b) ..... [2]

9 (a) Express  $\frac{1}{2x+1} + \frac{2}{3x-2}$  as a single fraction in its simplest form.

(b) Simplify  $\frac{a^3b^2c^3}{24c^4} \div \frac{a^3b}{8c}$

$$\frac{1}{2x+1} + \frac{2}{3x-2} = \frac{(3x-2)}{(2x+1)(3x-2)} + \frac{2(2x+1)}{(2x+1)(3x-2)} \quad [\text{M1}]$$

$$\begin{aligned} \text{(a)} \quad &= \frac{3x-2+4x+2}{(2x+1)(3x-2)} \\ &= \frac{7x}{(2x+1)(3x-2)} \quad [\text{A1}] \end{aligned}$$

$$\begin{aligned} \text{(b)} \quad \frac{a^3b^2c^3}{24c^4} \div \frac{a^3b}{8c} &= \frac{a^3b^2c^3}{24c^4} \times \frac{8c}{a^3b} \quad [\text{M1}] \\ &= \frac{b}{3} \quad [\text{A1}] \end{aligned}$$

Answer (a) ..... [2]

(b) ..... [2]

10 Simplify each of the following expressions.

(a)  $\frac{2n^2 + 3n}{16n + 24}$

(b)  $\frac{e^4 f^2 - e^3 f^3}{e^2 f^4 - e^3 f^3}$

(a)  $\frac{2n^2 + 3n}{16n + 24} = \frac{n(2n + 3)}{8(2n + 3)}$  [M1]  
 $= \frac{n}{8}$  [A1]

(b)  $\frac{e^4 f^2 - e^3 f^3}{e^2 f^4 - e^3 f^3} = \frac{e^3 f^2 (e - f)}{e^2 f^3 (f - e)}$  [M1]  
 $= -\frac{e(e - f)}{f(e - f)}$   
 $= -\frac{e}{f}$  [A1]

Answer (a) ..... [2]

(b) ..... [2]

11 Solve  $(x + 3)(x - 5) = 20$ .

$(x + 3)(x - 5) = 20$   
 $x^2 - 2x - 15 = 20$  [M1]

$x^2 - 2x - 35 = 0$

$(x - 7)(x + 5) = 0$  [M1]

$x = 7$  or  $-5$  [A1]

Answer  $x =$  ..... [3]

12 Given that  $p = \sqrt{\frac{2-q}{3+q}}$ ,

(a) find the value of  $p$  when  $q = -\frac{5}{2}$ ,

(b) express  $q$  in terms of  $p$ .

$$p = \sqrt{\frac{2 - \left(-\frac{5}{2}\right)}{3 + \left(-\frac{5}{2}\right)}}$$

(a)  $= \sqrt{\frac{\frac{9}{2}}{\frac{1}{2}}}$  [M1]

$= 3$  [A1]

$$p = \sqrt{\frac{2-q}{3+q}}$$

$$p^2 = \frac{2-q}{3+q}$$
 [M1]

$$p^2(3+q) = 2-q$$

(b)  $3p^2 + p^2q = 2 - q$

$$p^2q + q = 2 - 3p^2$$
 [M1]

$$q(p^2 + 1) = 2 - 3p^2$$

$$q = \frac{2 - 3p^2}{p^2 + 1}$$
 [A1]

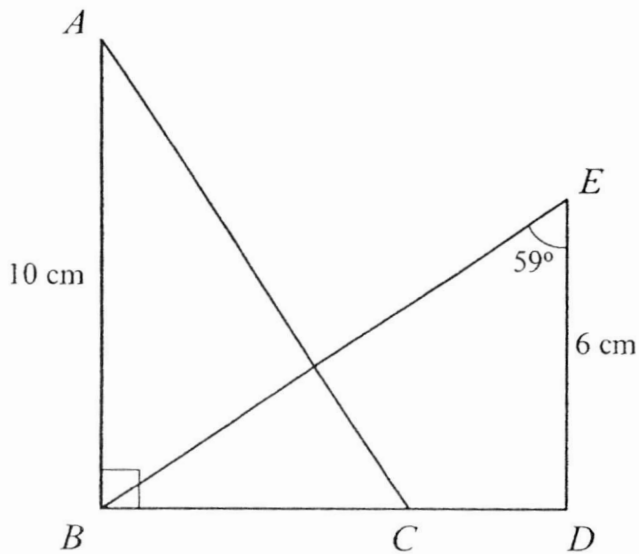
Answer (a)  $p = \dots\dots\dots$  [2]

(b)  $q = \dots\dots\dots$  [3]

- 13 In the figure below,  $\triangle ABC$  is congruent to  $\triangle BDE$ , and  
 $\angle ABC = 90^\circ$ ,  $\angle BED = 59^\circ$ ,  $AB = 10$  cm and  
 $DE = 6$  cm.

Find

- (a)  $\angle BAC$ ,  
 (b) the length of  $CD$ .



$$(a) \quad \angle DBE = 180^\circ - 90^\circ - 59^\circ \text{ (}\angle \text{sum of } \Delta\text{)}$$

$$\quad \quad \quad = 31^\circ \quad \quad \quad \text{[M1]}$$

$$\angle BAC = \angle DBE = 31^\circ \quad \quad \quad \text{[A1]}$$

- (b)  $\triangle ABC$  is congruent to  $\triangle BDE$  (given).

$$BD = AB = 10 \text{ cm}$$

$$BC = DE = 6 \text{ cm} \quad \quad \quad \text{[M1]}$$

$$CD = BD - BC$$

$$\quad \quad \quad = 10 - 6$$

$$\quad \quad \quad = 4 \text{ cm} \quad \quad \quad \text{[A1]}$$

Answer (a)  $\angle BAC = \dots\dots\dots$  [2]

(b)  $CD = \dots\dots\dots$  cm [2]

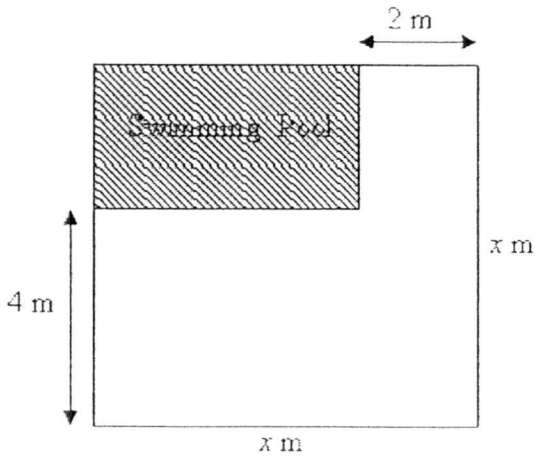
14 Ahmad decided to build a swimming pool in his house on a square plot of land of side  $x$  metres.

(a) Write down an expression, in terms of  $x$ , for the area of the swimming pool.

(b) The area of the swimming pool was found to be  $80 \text{ m}^2$ .

Show that  $x^2 - 6x - 72 = 0$ .

(c) Hence, find the value of  $x$ .



(a) 
$$\begin{aligned} \text{Area} &= (x-2)(x-4) \\ &= x^2 - 6x + 8 \end{aligned} \quad [\text{B1}]$$

(b) 
$$\begin{aligned} x^2 - 6x + 8 &= 80 \\ x^2 - 6x - 72 &= 0 \end{aligned} \quad [\text{B1}]$$

(c) 
$$\begin{aligned} x^2 - 6x - 72 &= 0 \\ (x-12)(x+6) &= 0 && [\text{M1}] \\ x &= 12 \text{ or } -6 \text{ (reject)} \\ &= 12 && [\text{A1}] \end{aligned}$$

Note: Award 1 Answer mark only if they reject  $x = -6$

Answer (a) Area = .....  $\text{m}^2$  [1]

(b) Answer to be shown above [1]

(c)  $x =$  ..... [2]

End of Paper





BEATTY SECONDARY SCHOOL  
MID-YEAR EXAMINATION 2015

SUBJECT : Mathematics

LEVEL : Sec 2 Express

PAPER : 2

DURATION : 1 hour 30 minutes

SETTER : Mrs Samsol

DATE : 18 May 2015

CLASS :	NAME :	REG NO :
---------	--------	----------

.....

**READ THESE INSTRUCTIONS FIRST**

Write your name, class and index number in the spaces on the top of this page.  
Write in dark blue or black pen.  
You may use a pencil for any diagrams or graphs.  
Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer **all** questions.

If working is needed for any question, it must be shown with the answer.  
Omission of essential working will result in loss of marks.  
Calculators should be used where appropriate.  
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.  
For  $\pi$ , use either your calculator value or 3.142, unless the question requires the answer in terms of  $\pi$ .

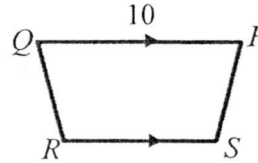
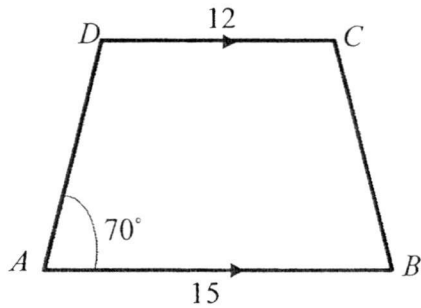
At the end of the examination, fasten all your work securely together.  
The number of marks is given in brackets [ ] at the end of each question or part question.  
The total number of marks for this paper is 50.

---

This paper consists of 5 printed pages (including this cover page)

1 Trapezium  $ABCD$  is similar trapezium  $PQRS$ .

Given that  $AB = 15$  cm,  $DC = 12$  cm,  $PQ = 10$  cm and  $\angle DAB = 70^\circ$ .



- (a) Identify the side in trapezium  $ABCD$  that corresponds to the side  $QR$  in trapezium  $PQRS$ . [1]
- (b) Find
- (i)  $\angle PSR$ , [1]
- (ii) the length of  $RS$ . [2]

2 A park has an area of  $6.4 \text{ km}^2$ . It is represented by an area of  $0.4 \text{ cm}^2$  on map A.

- (a) Find the scale of the map in the form  $1 : n$ . [2]
- (b) The length of a road on map A is 11 cm. Find its actual length in km. [1]
- (c) Find the area, in  $\text{cm}^2$ , of the park drawn on map B whose scale is  $1 : 50\,000$ . [2]

3 (a) Car A travels at a speed of  $(4u^2 + 3u)$  km/h for 2.5 hours.

Car B travels at a speed of  $(u^2 + 6u - 1)$  km/h for 2 hours.

Find an expression in terms of  $u$ , for the total distance travelled by cars A and B.

Simplify your answer. [3]

- (b) Given the formula  $P = \frac{5b - a}{2a + 1}$ , make  $a$  the subject. [3]

- 4 (a) It is given that  $x = 3$  is a root of the equation  $5x^2 + kx - 6 = 0$ , where  $k$  is a constant.
- (i) Find the value of  $k$ . [2]
- (ii) Find the other root of the equation. [2]
- (b) Express  $\frac{x-1}{x^2-x-6} - \frac{2}{x+2}$  as a single fraction. [3]
- 

- 5 (a) Factorise fully
- (i)  $36x^2 - 16$ , [2]
- (ii)  $2pq - 8p - 20 + 5q$ . [2]
- (b) Given that  $a^2 - b^2 = 24$  and  $a + b = 8$ , find the value of  $3a - 3b$ . [3]
- 

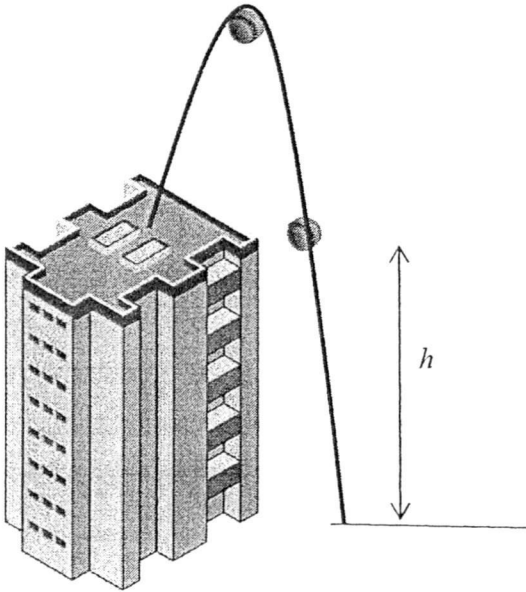
- 6 (a) It is given that  $A$  is directly proportional to the cube of  $r$ .  
Describe the change in the value of  $A$  when the value of  $r$  is doubled.  
Show working to support your answer. [2]
- (b)  $d$  is inversely proportional to  $x^n$ . The table below shows some values of  $x$  and the corresponding values of  $d$ .

$x$	1	2	5
$d$	40	10	$a$

- Find the value of  $n$  and of  $a$ . [3]
-

7 Answer the whole of this question on a sheet of graph paper.

A ball is thrown from the top of a building. Its vertical height  $h$ , in metres, above the ground at time  $t$  seconds during the flight is represented by the equation  $h = 20 + 5t - t^2$ .



Some corresponding values of  $t$  and  $h$  are given in the following table.

$t$	0	1	2	3	4	5	6	7
$h$	20	24	26	$p$	24	20	14	6

(a) Calculate the value of  $p$ . [1]

(b) Using a scale of 2 cm to represent 1 second, draw a horizontal  $t$ -axis for  $0 \leq t \leq 8$ .

Using a scale of 1 cm to represent 2 m, draw a vertical  $h$ -axis for  $0 \leq h \leq 30$ .

On your axes, plot the points given in the table and join them with a smooth curve. [3]

(c) Use your graph to estimate

(i) the maximum height of the ball from the ground, [1]

(ii) the time when the ball is 18 m above the ground. [1]

(d) Explain how you can use your graph to estimate the time when the ball hits the ground. [1]

(e) State the equation of the line of symmetry of the curve. [1]

8 (a) Expand and simplify  $3\left(\frac{1}{2}x + 5\right)^2 - 2\left(\frac{1}{3}x - 2\right)$ . [3]

(b) Simplify

(i)  $\frac{5a^3b}{9b^2c} \div \frac{10a}{3b}$ , [2]

(ii)  $\frac{2pq + 3q}{q^2} \times \frac{2p^2 - p - 3}{4p^2 - 9}$ . [3]

---

~ End of Paper ~

Answer Key

1(a) BC

1(b)(i)  $110^\circ$  (ii) 8 cm2(a) 1 : 400 000 (b) 44 km (c)  $25.6 \text{ cm}^2$ 3(a)  $(12u^2 + 19.5u - 2) \text{ km}$  (b)  $a = \frac{5b - P}{2P + 1}$ 4(a)(i)  $k = -13$  (ii)  $x = -\frac{2}{5}$ (b)  $\frac{5 - x}{(x - 3)(x + 2)}$ 5(a)(i)  $4(3x + 2)(3x - 2)$  (ii)  $(q - 4)(2p + 5)$ 

(b) 9

6(a)  $A$  increases by 8 times of the original value.

(b) 1.6

7(a) 26 (c)(i) 26.1 to 26.3 (ii) 5.3 to 5.5 (d) 7.5 to 7.7 (e)  $x = 2.5$ 8(a)  $\frac{3}{4}x^2 + \frac{43}{3}x + 79$ (b)(i)  $\frac{a^2}{6c}$ (ii)  $\frac{p + 1}{q}$

Mid-Year Exam 2015  
 Mathematics / Paper 2  
 Sec 2 Express  
 Setter : Mrs Samsol

Mark Scheme

**Deduct 1 mark overall for no units given for 1(b)(i), 3(a) , 7(c)(i),7(c)(ii)**

No	Workings	Marks	Remarks
1(a)	BC	B1	B0 if CB is given
1(b)(i)	$\angle PSR = \angle ADC = 180^\circ - 70^\circ$ int $\angle$ s) $= 110^\circ$	B1	<b>B0 if sum of quad is used.</b> <b>B0 if incorrect corresponding angle is stated even if answer given is <math>110^\circ</math></b>
1(b)(ii)	$\frac{RS}{CD} = \frac{PQ}{AB}$  $\frac{RS}{12} = \frac{10}{15}$ $RS = \frac{10}{15} \times 12$ $= 8 \text{ cm}$	M1    A1	
2(a)	$0.4 \text{ cm}^2 : 6.4 \text{ km}^2$ $1 \text{ cm}^2 : 16 \text{ km}^2$ $1 \text{ cm} : 4 \text{ km}$ $1 \text{ cm} : 400\,000 \text{ cm}$ $1 : 400\,000$	M1   A1	
2(b)	Actual length = $11 \times 4$ $= 44 \text{ km}$	B1	B0 if no units or wrong units
2(c)	Map B : $1 \text{ cm} : 50\,000 \text{ cm}$ $1 \text{ cm} : 0.5 \text{ km}$ $1 \text{ cm}^2 : 0.25 \text{ km}^2$  Map area = $\frac{6.4}{0.25}$  $= 25.6 \text{ cm}^2$	M1   A1	A0 if no units or wrong units

3(a)	Total distance $= 2.5(4u^2 + 3u) + 2(u^2 + 6u - 1)$  $= 10u^2 + 7.5u + 2u^2 + 12u - 2$  $= (12u^2 + 19.5u - 2) \text{ km}$	M1  M1  A1	
3(b)	$P = \frac{5b - a}{2a + 1}$  $P(2a + 1) = 5b - a$ $2aP + P = 5b - a$ $2aP + a = 5b - P$ $a(2P + 1) = 5b - P$ $a = \frac{5b - P}{2P + 1}$	M1  M1 ( factorisation)  A1	
4(a)(i)	$5(3)^2 + 3k - 6 = 0$ $3k = -39$ $k = -13$	M1  A1	
4(a)(ii)	$5x^2 - 13x - 6 = 0$ $(5x + 2)(x - 3) = 0$ $x = -\frac{2}{5} \text{ or } x = 3 \text{ (reject)}$	M1  A1	If $k = 13$ , give M1√ for correct factorisation
4(b)	$\frac{x-1}{x^2-x-6} - \frac{2}{x+2}$ $= \frac{x-1}{(x-3)(x+2)} - \frac{2}{x+2}$ $= \frac{x-1}{(x-3)(x+2)} - \frac{2(x-3)}{x+2}$ $= \frac{x-1-2x+6}{(x-3)(x+2)}$ $= \frac{5-x}{(x-3)(x+2)}$	M1 (factorise)  M1 (Correct expansion)  A1	

5(a)(i)	$36x^2 - 16$ $= 4(9x^2 - 4)$ $= 4(3x+2)(3x-2)$	M1 A1	
5(a)(ii)	$2pq - 8p - 20 + 5q$ $= 2p(q-4) - 5(4-q)$ $= 2p(q-4) + 5(q-4)$ $= (q-4)(2p+5)$	M1  A1	<p>Rearranging may be done at the first step :</p> $2pq - 8p + 5q - 20$ $= 2p(q-4) + 5(q-4)$ M1 Give M0 if $2p(q-4)[-5(4-q)]$ is seen
5(b)	$a^2 - b^2 = 24$ $(a+b)(a-b) = 24$ $8(a-b) = 24$ $a-b = 3$ $3a - 3b = 3(a-b)$ $= 3(3)$ $= 9$	M1  M1  A1	
6(a)	Let $A = kr^3$ $A = k(2r)^3$ $A = 8kr^3$  $A$ is 8 times of the original value. or $A$ increases by 700% or increases by 7 times .	M1  A1	
6(b)	Let $d = d = \frac{k}{x^n}$ $40 = \frac{k}{1}$ $k = 40$ Sub $x = 2$ and $d = 10$ $10 = \frac{40}{2^n}$ $2^n = 4 = 2^2$ $n = 2$ $a = \frac{40}{5^2} = \frac{8}{5} \text{ or } 1.6$	B1  B1  B1	

7(a)	$p = 26$	B1	
7(b)	Refer to graph	G1:Correct scale and <b>correct label of both axes</b> G1:All points plotted correctly G1:Smooth curve	
7(c)(i)	26.25 m ( Accept 26.1 to 26.5)	B1	
7(c)(ii)	5.4 s (Accept 5.3 to 5.5)	B1	
7(d)	Extend the graph until it meets the t-axis. The t-value is the time required.	B1	
7(e)	$t = 2.5$	B1	
8(a)	$3\left(\frac{1}{2}x + 5\right)^2 - 2\left(\frac{1}{3}x - 2\right)$ $= 3\left(\frac{1}{4}x^2 + 5x + 25\right) - \frac{2}{3}x + 4$ $= \frac{3}{4}x^2 + 15x + 75 - \frac{2}{3}x + 4$ $= \frac{3}{4}x^2 + \frac{43}{3}x + 79$	M1 M1 A1	
8(b)(i)	$\frac{5a^3b}{9b^2c} \div \frac{10a}{3b}$ $= \frac{5a^3b}{9b^2c} \times \frac{3b}{10a}$ $= \frac{a^2}{6c}$	M1 A1	
8(b)(ii)	$\frac{2pq + 3q}{q^2} \times \frac{2p^2 - p - 3}{4p^2 - 9}$ $= \frac{q(2p + 3)}{q^2} \times \frac{(2p - 3)(p + 1)}{(2p + 3)(2p - 3)}$ $= \frac{p + 1}{q}$	M1 (factorization of numerator) M1 (factorization of numerator) A1	

For  
Examiner's  
useFor  
Examiner's  
use

1. Express 112% as
- a decimal,
  - a mixed number in the lowest term,
  - an improper fraction in the lowest term.

Answer (a) \_\_\_\_\_ [ 1 ]

(b) \_\_\_\_\_ [ 1 ]

(c) \_\_\_\_\_ [ 1 ]

2. Solve the equation  $\frac{x+3}{4} = \frac{2x-3}{5}$ .

Answer  $x =$  \_\_\_\_\_ [ 2 ]

3. Consider the pattern

$$1^2 - 0^2 = 1$$

$$2^2 - 1^2 = 3$$

$$3^2 - 2^2 = 5$$

$$4^2 - 3^2 = 7$$

.

.

.

$$x^2 - y^2 = 101$$

.

.

.

- Write down the seventh line in the pattern.
- Find the integer values of  $x$  and  $y$  which satisfy the equation  $x^2 - y^2 = 101$ .

Answer (a) \_\_\_\_\_ [ 1 ]

(b)  $x =$  \_\_\_\_\_,  $y =$  \_\_\_\_\_ [ 2 ]

For  
Examiner's  
useFor  
Examiner's  
use

4. (a) Round off the following numbers correct to 3 significant figures.  
 (i) 1.998  
 (ii) 3.002
- (b) Hence, estimate the value of  $\frac{1.998 \times 3.002}{\sqrt[3]{217}}$ .

Answer (a) (i) \_\_\_\_\_ [ 1 ]

(ii) \_\_\_\_\_ [ 1 ]

(b) \_\_\_\_\_ [ 2 ]

5. A map is drawn to a scale of 1 : 250 000. A city covers an area of  $700 \text{ km}^2$ . Find, in  $\text{cm}^2$ , the area representing the city on the map.

Answer \_\_\_\_\_  $\text{cm}^2$  [ 2 ]

6. Simplify  $\frac{20n^3}{3m^3} \times \frac{6m^2n}{25n^4}$ , giving your answer in the lowest terms.

Answer \_\_\_\_\_ [ 2 ]

For  
Examiner's  
useFor  
Examiner's  
use

7. The volume of air,  $V \text{ cm}^3$ , inside a bicycle pump is inversely proportional to the cube root of the air pressure,  $P$  units. It is given that the air pressure is 1728 units when  $15 \text{ cm}^3$  of air is pumped. Find
- (a) an equation connecting  $V$  and  $P$ .

Answer (a) \_\_\_\_\_ [ 2 ]

- (b) the volume of air that is pumped when the pressure is 216 units.

Answer (b) \_\_\_\_\_  $\text{cm}^3$  [ 1 ]

- (c) the air pressure when  $22.5 \text{ cm}^3$  of air is pumped.

Answer (c) \_\_\_\_\_ units [ 1 ]

8. Express  $\frac{3}{x+1} - \frac{2}{3x+2}$  as a single fraction in its simplest form

Answer \_\_\_\_\_ [ 2 ]

For  
Examiner's  
use

For  
Examiner's  
use

9. Given that  $A = \frac{1}{2}h(a + b)$ ,
- (a) find the value of  $A$  when  $h = 4$ ,  $a = 5$  and  $b = 7$ ,
- (b) express  $h$  in terms of  $A$ ,  $a$  and  $b$ .

Answer (a)  $A =$  \_\_\_\_\_ [ 1 ]

(b) \_\_\_\_\_ [ 2 ]

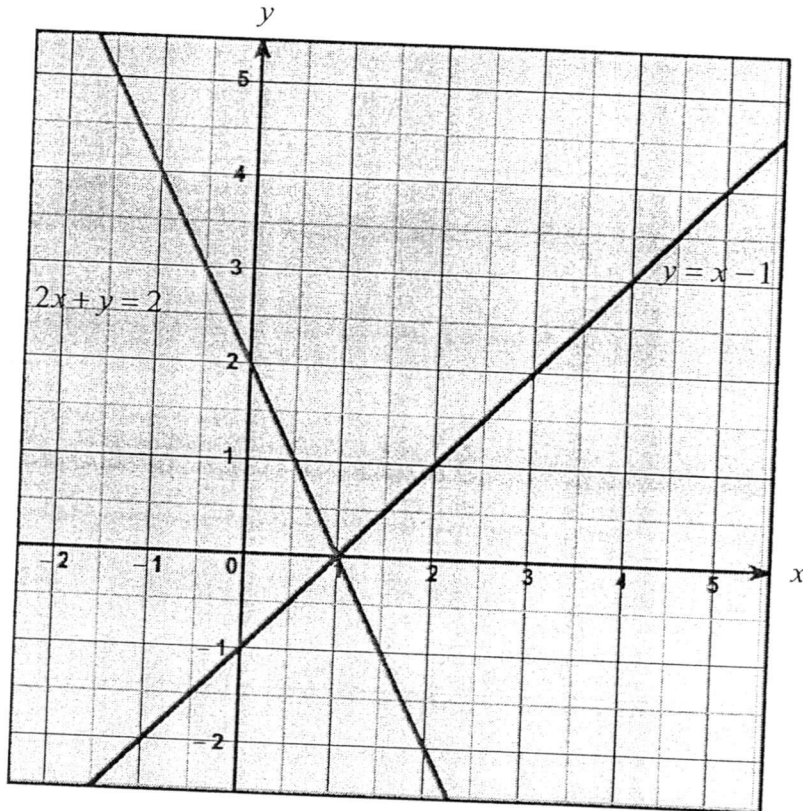
10. (a) Factorize  $w^2 - 13w + 36$ .
- (b) (i) Factorize  $u^2 - v^2$ .
- (ii) Given that  $u - v = 8$  and  $u^2 - v^2 = 28$ , find the value of  $u + v$ .

Answer (a) \_\_\_\_\_ [ 1 ]

(b) (i) \_\_\_\_\_ [ 1 ]

(ii) \_\_\_\_\_ [ 2 ]

11. The graph below shows the lines  $y = x - 1$  and  $2x + y = 2$ .



- (a) State the solution of the simultaneous equations  $y = x - 1$  and  $2x + y = 2$ .

Answer (a)  $x = \underline{\hspace{1cm}}$ ,  $y = \underline{\hspace{1cm}}$  [ 2 ]

- (b) On the same grid above, draw and label clearly the line  $y = 2$ . [ 1 ]

- (c) Find the area of the polygon enclosed by the 3 lines,  $y = x - 1$ ,  $2x + y = 2$  and  $y = 2$ . Leave your answer in square units.

Answer (c)  $\underline{\hspace{1cm}}$  units<sup>2</sup> [ 1 ]

12. Solve  $2x + y = 5$  and  
 $x + 2y = 7$ .

Answer  $x = \underline{\hspace{1cm}}$ ,  $y = \underline{\hspace{1cm}}$  [ 3 ]

For  
Examiner's  
use

13. Solve the following equations.

(a)  $(x - 5)^2 = 100$

(b)  $y^2 + 3y - 700 = 0$

For  
Examiner's  
use

Answer (a)  $x =$  \_\_\_\_\_ [ 2 ]

(b)  $y =$  \_\_\_\_\_ [ 2 ]

14. If 5 men take 6 days to complete a task,

(a) how many days would 3 men take,

(b) how many men would be needed to complete the task in 2 days?

Answer (a) \_\_\_\_\_ days [ 2 ]

(b) \_\_\_\_\_ men [ 2 ]

For  
Examiner's  
use

15. Expand and simplify

(a)  $(2a + 3)^2 + 4a(1 - a)$

For  
Examiner's  
use

Answer (a) \_\_\_\_\_ [2]

(b)  $\left(\frac{x^2}{3} - 3\right)^2$

Answer (b) \_\_\_\_\_ [2]

(c)  $(2y - 1)^2 - (3y + 1)(4y - 1)$

Answer (c) \_\_\_\_\_ [2]

End of paper

## Answer key

1a.	1.12
1b.	$1\frac{3}{25}$
1c.	$\frac{28}{25}$
2.	9
3a.	$7^2 - 6^2 = 13$
3b.	$x = 51, y = 50$
4a.	( i ) 2.00 ( ii ) 3.00
4b.	1
5.	$112 \text{ cm}^2$
6.	$\frac{8}{5m}$
7a.	$V = \frac{180}{\sqrt[3]{P}}$
7b.	$30 \text{ cm}^3$
7c.	512 units
8.	$\frac{7x+4}{(x+1)(3x+2)}$
9a.	24
9b.	$h = \frac{2A}{a+b}$
10a.	$(w-4)(w-9)$
10b.	( i ) $(u-v)(u+v)$ ( ii ) 3.5
11a.	$x = 1, y = 0$

11c.	$3 \text{ units}^2$
12.	$x = 1, y = 3$
13a.	$x = 15 \text{ or } -5$
13b.	$y = 25 \text{ or } -28$
14a.	10
14b.	15
15a.	$16a + 9$
15b.	$\frac{x^4}{9} - 2x^2 + 9$
15c.	$-8y^2 - 5y + 2$