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**SECONDARY 4
PRELIMINARY EXAMINATION
MATHEMATICS
Paper 1**

4048/01

1 September 2020 (Tuesday)

2 hours

CANDIDATE
NAME

CLASS

INDEX
NUMBER

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READ THESE INSTRUCTIONS FIRST

Do not turn over the page until you are told to do so.
Write your name, class and index number in the spaces above.
Write in dark blue or black pen in the space provided.

You may use a pencil for any diagrams or graphs.
Do not use staples, paper clips, glue or correction fluid.

INFORMATION FOR CANDIDATES

Answer **all** the questions.

If working is needed for any question it must be shown with the answer.

Omission of essential working will result in loss of marks.

The use of an approved scientific calculator is expected, where appropriate.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures.
Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142, unless the question requires the answer in terms of π .

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is **80**.

For Examiner's Use		
Q1	2	
Q2	2	
Q3	2	
Q4	2	
Q5	2	
Q6	3	
Q7	3	
Q8	3	
Q9	3	
Q10	3	
Q11	3	
Q12	4	
Q13	4	
Q14	4	
Q15	4	
Q16	4	
Q17	5	
Q18	5	
Q19	5	
Q20	5	
Q21	6	
Q22	6	
Total	/ 80	

MATHEMATICAL FORMULAE

Compound interest

$$\text{Total amount} = P \left(1 + \frac{r}{100} \right)^n$$

Mensuration

$$\text{Curved surface area of a cone} = \pi r l$$

$$\text{Surface area of a sphere} = 4\pi r^2$$

$$\text{Volume of a cone} = \frac{1}{3} \pi r^2 h$$

$$\text{Volume of a sphere} = \frac{4}{3} \pi r^3$$

$$\text{Area of triangle } ABC = \frac{1}{2} ab \sin C$$

$$\text{Arc length} = r\theta, \text{ where } \theta \text{ is in radians}$$

$$\text{Sector area} = \frac{1}{2} r^2 \theta, \text{ where } \theta \text{ is in radians}$$

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

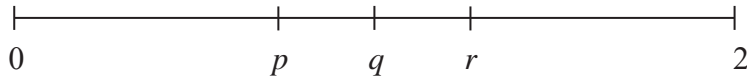
Statistics

$$\text{Mean} = \frac{\sum fx}{\sum f}$$

$$\text{Standard deviation} = \sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f} \right)^2}$$

Answer **all** the questions.

- 1 The numbers p , q and r are represented on the number line.



The values of p , q , and r are listed below.

$$\left(-\frac{2}{3}\right)^0 \quad \frac{\pi}{2} \quad \frac{5}{8} \quad \sqrt{5}$$

- (a) Find p , q and r .

Answer $p = \dots\dots\dots$

$q = \dots\dots\dots$

$r = \dots\dots\dots$ [1]

- (b) Write down the irrational number(s).

Answer $\dots\dots\dots$ [1]

- 2 A Shinkansen train 273 m long passes through a tunnel 2 km long. The average speed of the train is 240 km/h.

Calculate the time taken for the train to pass through the tunnel completely.
Give your answer in seconds.

Answer $\dots\dots\dots$ seconds [2]

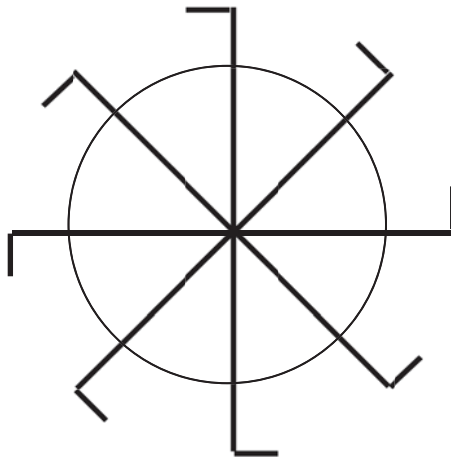
[Turn over

- 3 It is given that $w = \frac{4a - 3b}{b + c}$.

Express b in terms of w , a and c .

Answer $b = \dots\dots\dots$ [2]

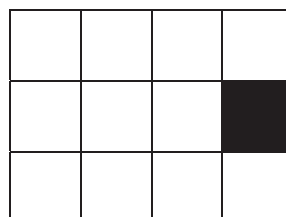
- 4 (a) The diagram shows a simplified view of a waterwheel.



State the order of rotational symmetry.

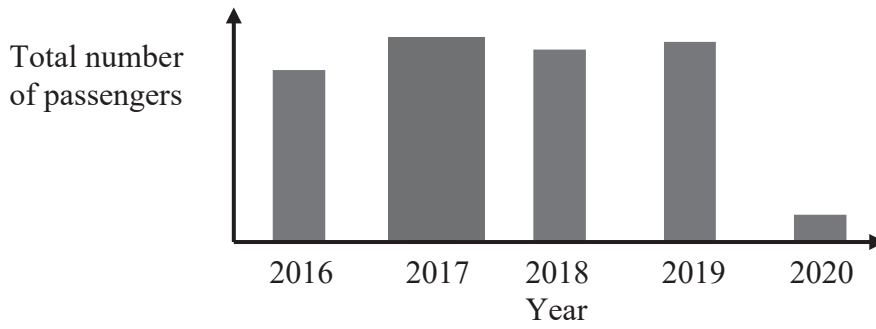
Answer $\dots\dots\dots$ [1]

- (b) Shade one more square on the diagram, such that the diagram has two lines of symmetry.



[1]

- 5 The chart shows the total number of passengers at Changi Airport in the years 2016 to February 2020.



State one feature of the chart that may be misleading and explain why.

.....

.....

..... [2]

- 6 Simplify

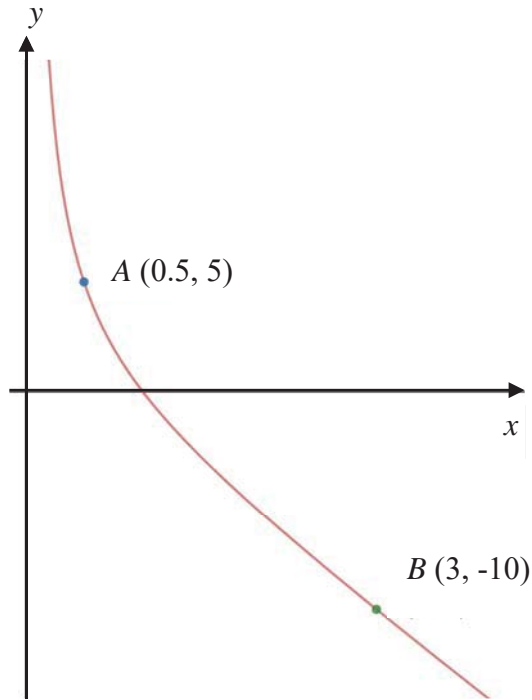
(a) $a^2b \times a^{-2}b^5$,

Answer [1]

(b) $\left(\frac{27}{x^{18}}\right)^{-\frac{1}{3}}$.

Answer [2]

- 7 The sketch below shows the graph of $y = \frac{p}{x} + qx + 1$.
The points $A(0.5, 5)$ and $B(3, -10)$ lie on the graph.
Find the values of p and q .



Answer $p = \dots\dots\dots$
 $q = \dots\dots\dots$

[3]

[Turn over

8 $\xi = \{\text{integers } x : 1 \leq x \leq 20\}$

$P = \{\text{prime numbers}\}$

$Q = \{\text{multiples of 3}\}$

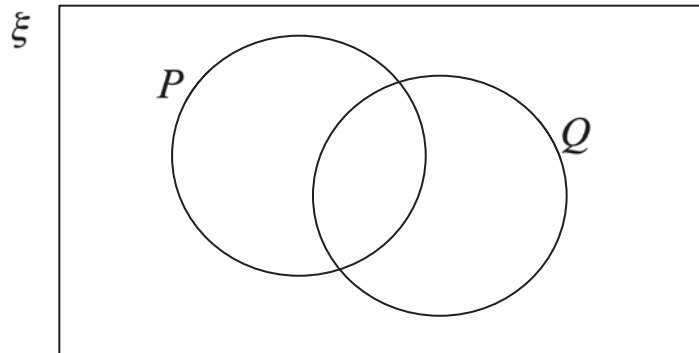
(a) List the element(s) in $P \cap Q$.

Answer [1]

(b) Circle the correct statement from the list below.

$P \subset Q$ $Q \cap P' \neq \phi$ $(Q \cup P)' = \{1\}$ [1]

(c) On the Venn diagram, shade the region that represents $P \cup Q'$.



[1]

- 9 Jen wants to buy a vacuum cleaner costing \$480.
Covey Norm departmental store has a payment plan for customers to pay a deposit of \$100 and then 24 monthly payments, each of 4% of the original cost of the vacuum cleaner.
How much more than the original cost will Jen pay if she uses the payment plan?

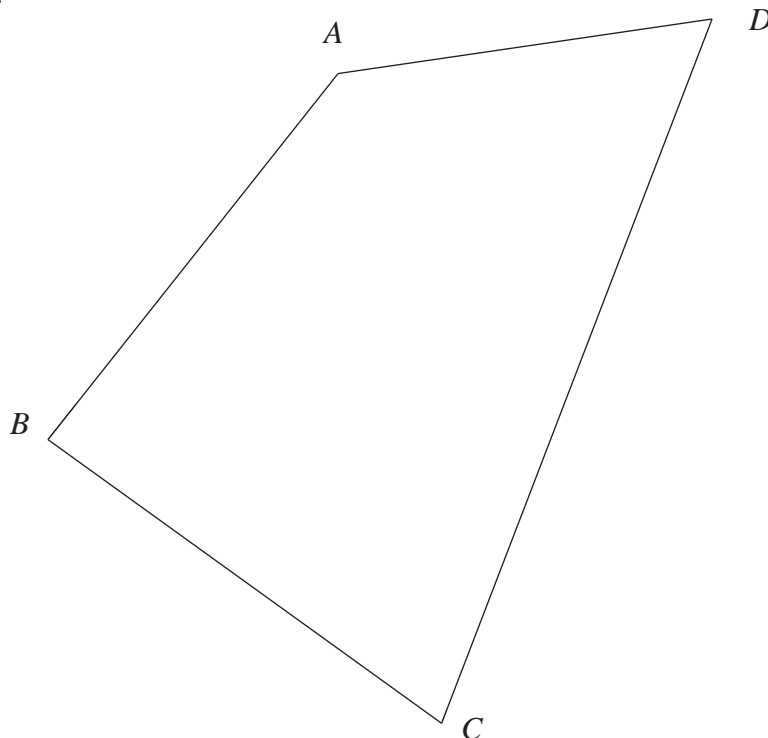
Answer \$..... [3]

- 10 The scale drawing in the answer space below shows a piece of land $ABCD$.
The owner of the land decides to use part of the land to build a nursery based on the following requirements:

- (i) The nursery is closer to the line AB than AD
- (ii) The nursery is closer to the point D than C

By constructing an angle bisector and a perpendicular bisector, shade the area of the land where the nursery will be built.

Answer

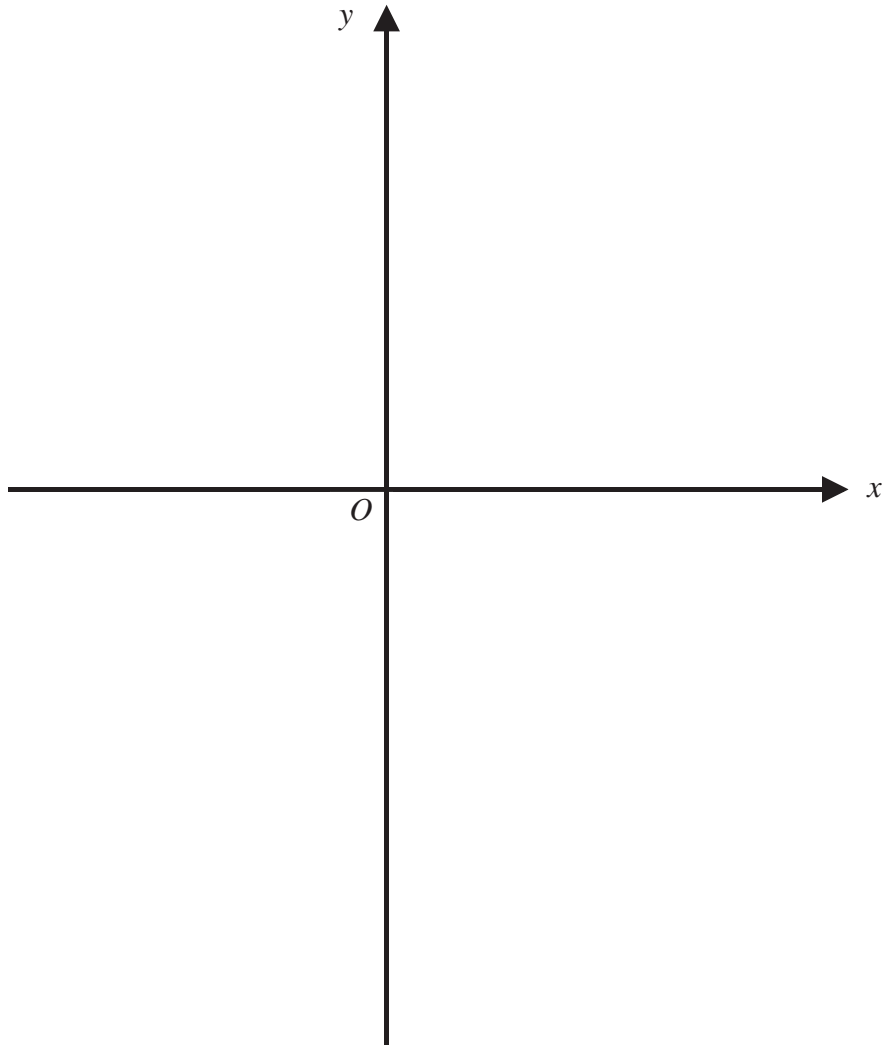


[3]

11 **Sketch** the graph of $y = 9 - (x - 1)^2$ on the axes below.

Indicate clearly the coordinates of the points where the graph crosses the axes and the maximum point on the curve.

Answer

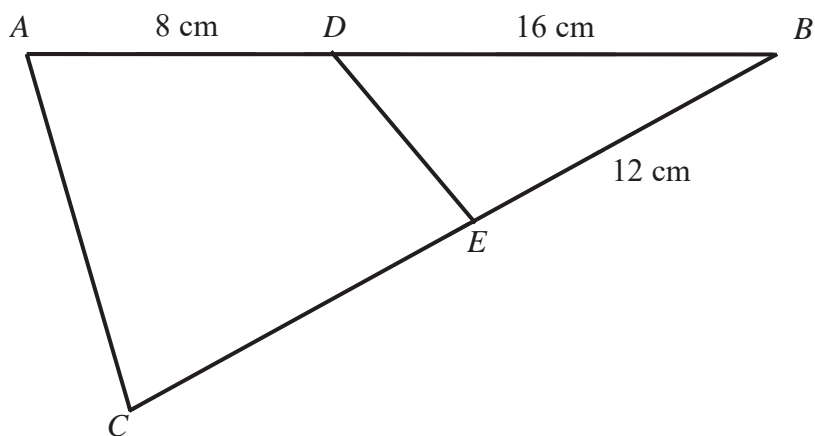


[3]

[Turn over

- 12 In the diagram D and E are points on AB and BC respectively such that angle $BDE =$ angle BCA .

$BD = 16$ cm, $DA = 8$ cm and $BE = 12$ cm.



- (a) Show that triangle BDE and triangle BCA are similar.

Answer (a) In triangle BDE and triangle BCA

.....

.....

.....

[2]

- (b) Hence, find EC .

Answer $EC = \dots\dots\dots$ cm

[2]

- 13 (a) (i) Express 84 as the product of its prime factors.

Answer [1]

- (ii) The number $\frac{84h}{g}$ is a perfect square.

h and g are prime numbers such that $h < g$.

Find the value of h and the value of g .

Answer $h =$

$g =$ [1]

- (b) Find two numbers, except 360 and 24, that have a lowest common multiple of 360 and a highest common factor of 24.

Answer , [2]

14 Factorise completely

(a) $2ax - x - a + 2x^2$.

Answer [2]

(b) $4y^3 - 16yx^2$.

Answer [2]

[Turn over

- 15 A polygon has n sides. Two of its exterior angles are 21° and 54° .
The remaining exterior angles are 15° each.
Find

(a) the value of n ,

Answer $n = \dots\dots\dots$ [2]

(b) the sum of interior angles of the polygon.

Answer $\dots\dots\dots^\circ$ [2]

- 16 (a) 4 skilled workers can complete a job in 5 days. 5 semi-skilled workers can complete the same job in 6 days. How long does it take 1 skilled worker and 1 semi-skilled worker to complete the same job if they work together?

Answerdays [2]

- (b) It is given that y is directly proportional to the square of x and $y = p$ for a particular value of x . Express y in terms of p when this value of x is halved.

Answer $y =$ [2]

[Turn over

17 The ratio of the base areas of two geometrically similar cylinders is 9:25.

(a) If the surface area of the smaller cylinder is 480 cm^2 , what is the surface area of the larger cylinder?

Answer cm^2 [2]

(b) Find the ratio of the heights of the two cylinders.

Answer [1]

(c) Both cylinders are filled with silica. The mass of the silica in the larger cylinder is 36 kg. Find the mass of silica in the smaller cylinder.

Answerkg [2]

[Turn over

18 A is the point $(3, 2)$ and B is the point $(9, -1)$

(a) Find the length of the line AB .

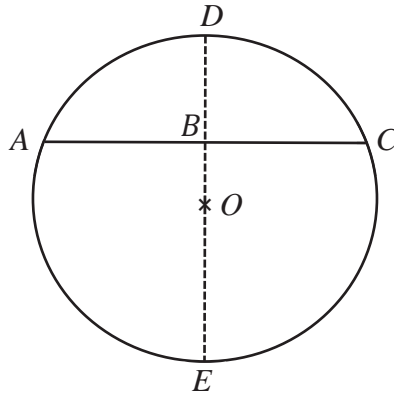
Answerunits [2]

(b) Find the equation of the straight line that is parallel to AB , and passes through point $C(-4, 0)$.

Answer [3]

[Turn over

- 19 The diagram shows a circle, centre O , radius 16 cm.
 B is the mid-point of the chord AC , DE is a diameter and $BE = 25$ cm.



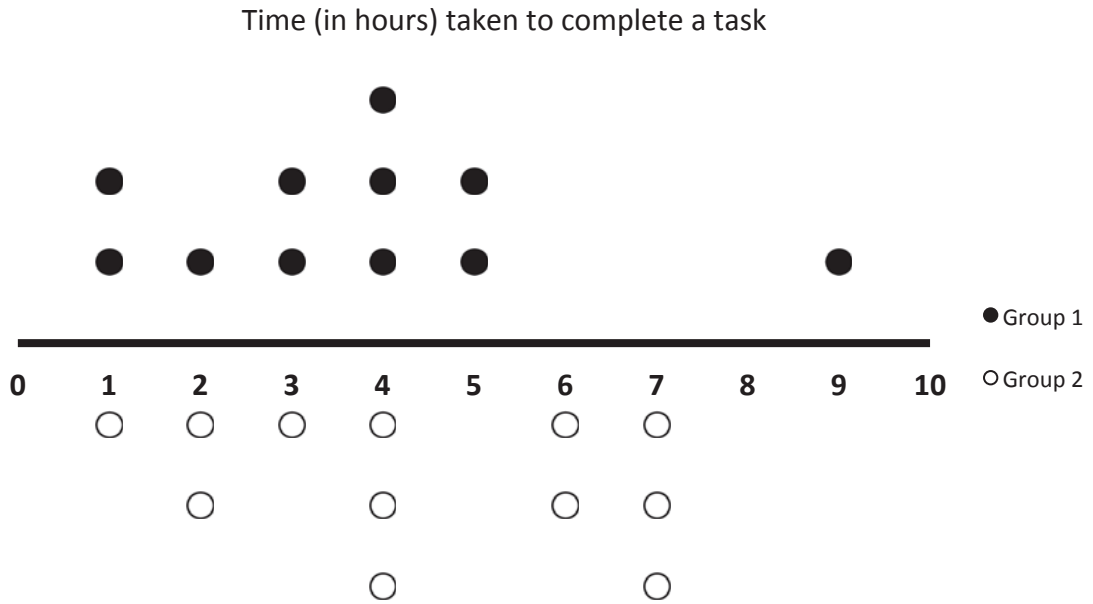
- (a) Calculate angle AOC in radian.

Answer [2]

- (b) Hence, find the area of the segment $ABCE$.

Answer cm^2 [3]

- 20 The time taken to complete a task by two groups of students, Group 1 and Group 2, were recorded.
The results are shown in the dot diagram.



- (a) Write down the median time taken by Group 1.

Answer hours [1]

- (b) Write down the range of the time taken by Group 2.

Answer hours [1]

- (c) Alice claims that Group 2 took a shorter time to complete the task as the range of the time taken by Group 2 is shorter than that of Group 1. Do you agree? Justify your answer.

I because

..... [2]

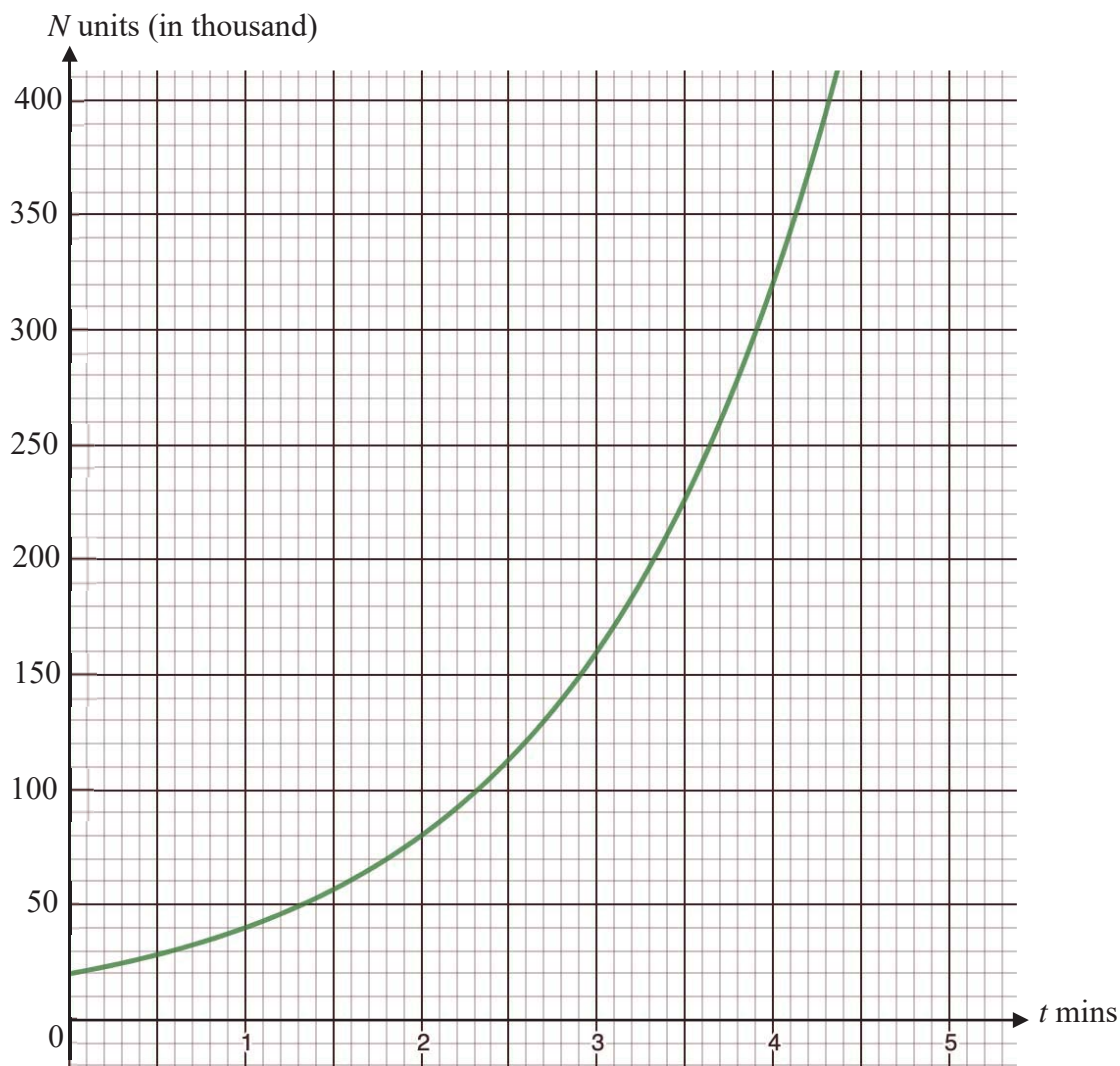
- (d) Which group's timing was more consistent? Justify your answer.

Answer (d) Group 's timing was more consistent because

..... [1]

- 21 The number of bacteria, N units (in thousand), in a food item after t minutes, are connected by the equation $N = 40(2^{t-1})$.

The graph $N = 40(2^{t-1})$ is drawn on the grid below.



- (a) Use the graph to estimate the range of values of t such that $80 < N < 320$.

Answer [1]

- (b) (i) By drawing a tangent, find the gradient of the curve at $(1, 40)$.

Answer [2]

(ii) Hence, state what the tangent at (1, 40) represents.

Answer [1]
.....

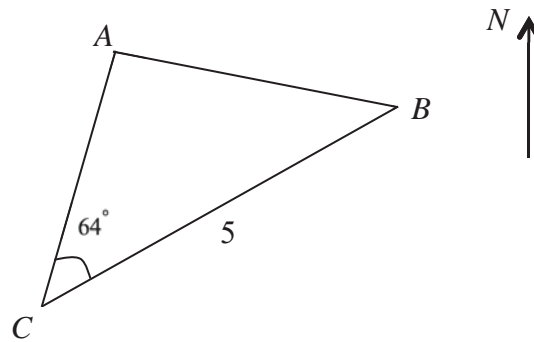
(iii) The food item is not safe to be consumed when the number of bacteria is at least 800% from its original amount.

Using the graph, determine after how long the food item is no longer safe to be consumed.

Answermin [2]

22 In the diagram, ABC represents a horizontal triangular garden.
 $CB = 5$ m.

Angle $ACB = 64^\circ$ and the bearing of A from B is 280° .



(a) Calculate the bearing of B from A .

Answer° [1]

(b) A vertical tree, BT , has its base at B .

The angle of depression of the point C when viewed from the top of the tree is 24° .

(i) Find the height of the tree.

Answerm [2]

(ii) David measured the largest angle of elevation of the top of the tree as seen from the path AC .

Calculate this angle of elevation.

Answer° [3]

MATHEMATICS
PAPER 2
SECONDARY 4
2020 PRELIMINARY EXAMINATION

4048/2

2 September 2020 (Wednesday)

2 hours 30 minutes

CANDIDATE
NAME

CLASS

INDEX
NUMBER

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The number of marks is given in brackets [] at the end of each question or part question.
The total number of marks for this paper is **100**.

For Examiner's Use		
Q1	10	
Q2	4	
Q3	5	
Q4	6	
Q5	9	
Q6	8	
Q7	10	
Q8	8	
Q9	9	
Q10	10	
Q11	11	
Q12	10	
Total	/100	

*Mathematical Formulae**Compound Interest*

$$\text{Total amount} = P \left(1 + \frac{r}{100} \right)^n$$

Mensuration

$$\text{Curved surface area of a cone} = \pi r l$$

$$\text{Surface area of a sphere} = 4\pi r^2$$

$$\text{Volume of a cone} = \frac{1}{3} \pi r^2 h$$

$$\text{Volume of a sphere} = \frac{4}{3} \pi r^3$$

$$\text{Area of triangle } ABC = \frac{1}{2} ab \sin C$$

$$\text{Arc length} = r\theta, \text{ where } \theta \text{ is in radians}$$

$$\text{Sector area} = \frac{1}{2} r^2 \theta, \text{ where } \theta \text{ is in radians}$$

Trigonometry

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^2 = b^2 + c^2 - 2bc \cos A$$

Statistics

$$\text{Mean} = \frac{\sum fx}{\sum f}$$

$$\text{Standard deviation} = \sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f} \right)^2}$$

Answer all questions.

1 (a) Solve the equation $\frac{a^2}{7} = \frac{a}{3}$.

Answer $a = \dots\dots\dots$ [3]

(b) Solve the inequalities $-2 < \frac{7x+3}{2} \leq 3-x$.

Answer $\dots\dots\dots$ [3]

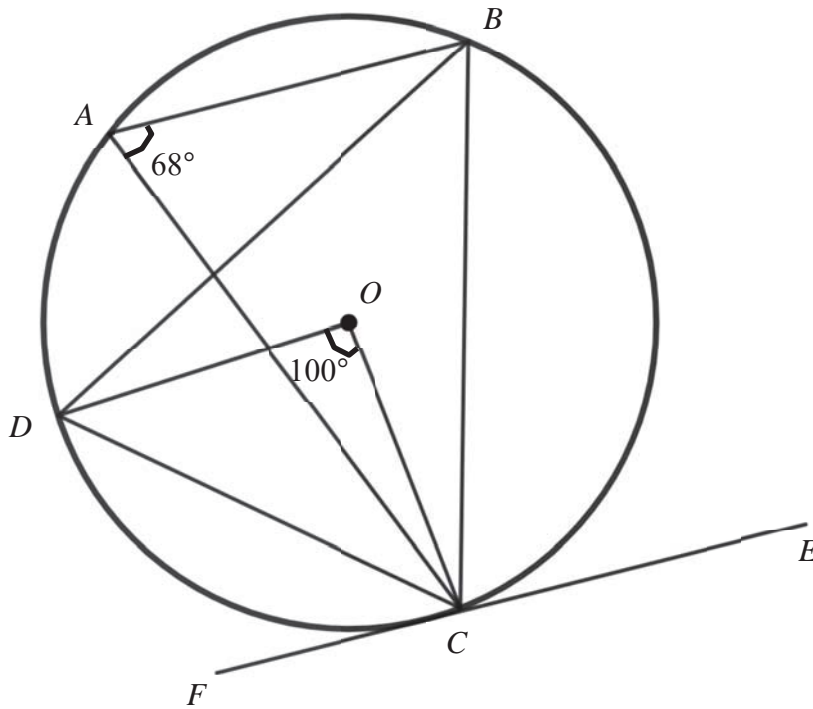
[Turn over

- (c) Express $\frac{6}{18d^2 - 30d + 8} + \frac{3}{16 - 9d^2}$ as a single fraction in its simplest form.

Answer [4]

[Turn over

- 2 In the diagram below, A, B, C and D are points on the circumference of a circle of centre O . FCE is a tangent to the circle at C . Angle $BAC = 68^\circ$ and angle $DOC = 100^\circ$



Find, giving reasons for each answer,

- (i) angle DBC ,

Answer [1]

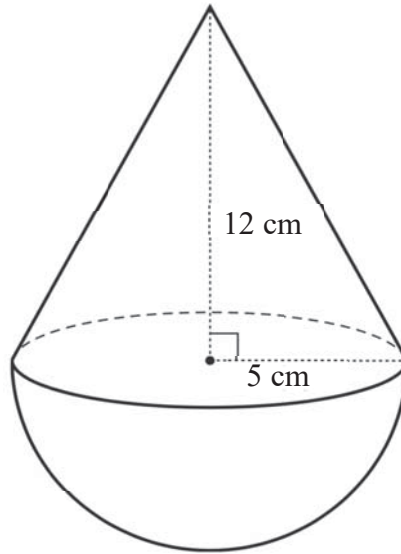
- (ii) angle DCF

Answer [1]

- (iii) angle BDO .

Answer [2]

- 3 The diagram shows a solid made up of a cone and a hemisphere. The hemisphere has a radius of 5 cm. The cone has a base radius of 5 cm and a height of 12 cm.



- (a) Calculate the surface area of the solid.

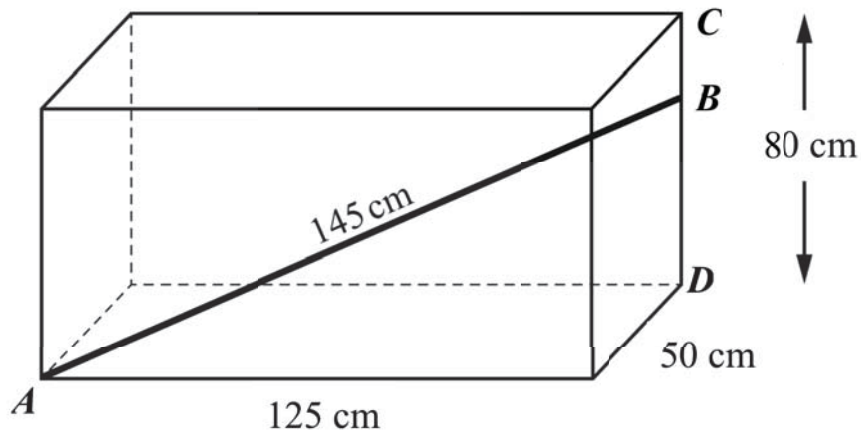
Answer cm^2 [3]

[Turn over

(b) Calculate the volume of the solid.

Answer cm^3 [2]

4



A piece of steel rod AB is placed in a box as shown above. AB is 145 cm. One end of the steel rod, A , is in the bottom corner of the box and the other end of the steel rod, B , is below the top corner of the box.

It is given that the box has a height of 80 cm, length of 125 cm and width of 50 cm.

(a) Find the length of BD .

Answercm [3]

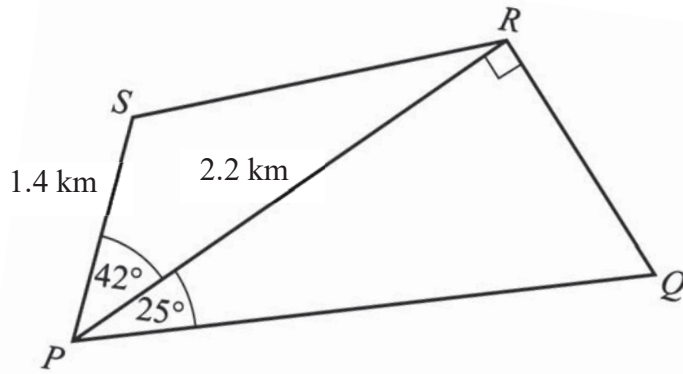
[Turn over

(b) Find the angle ABC .

Answer° [3]

[Turn over

- 5 The diagram shows a plot of land that is in the shape of a quadrilateral $PQRS$ where $PR = 2.2$ km and $PS = 1.4$ km. Angle $PRQ = 90^\circ$, angle $RPQ = 25^\circ$ and angle $SPR = 42^\circ$.



- (a) Calculate the length of QR .

Answerkm [2]

- (b) Calculate the area of the plot of land.

Answerkm² [3]

[Turn over

- (c) Determine whether it is possible to build a circular fence such that points P , Q , R and S lie on the circumference of a circle.
Justify your decision and show your calculations clearly.

Answer

.....

.....[4]

6 Ben has just relocated back to Singapore from United Kingdom.

- (a) Ben converted his savings of £50 000 to Singapore dollars when the exchange rate between pounds (£) and Singapore dollars (S\$) was £1 = S\$1.78. Calculate the amount of money in Singapore dollars Ben received after the conversion.

Answer S\$..... [1]

- (b) Ben is intending to invest this sum of money in a fixed deposit called the “*Multiply Plan*” for a period of one year. The interest earned from the “*Multiply Plan*” is compounded monthly based on the interest rates listed below.

<i>Multiply Plan</i>	
Interest rate for first six-month period	2% per annum
Interest rate for next six-month period	2.5% per annum (based on total amount at the end of the first six months)

Calculate the total amount of money in Singapore dollars that Ben would have at the end of one year, correct to the nearest cent.

Answer S\$..... [3]

[Turn over

- (c) Prior to returning to Singapore, Ben worked out a projected monthly expenditure for living in Singapore.

Rental of a HDB flat	S\$2200
Food	S\$400
Transport	S\$100
Leisure	S\$500

However, he realised that his actual monthly expenditure was different from his projected amount. He has to pay 25% more for rental of a flat, 40% more for food and 30% more for transport than what he had projected.

In order to reduce his monthly expenditure, he decided to cut back his monthly expenses for leisure by 50%.

- (i) Calculate Ben's actual monthly expenditure.

Answer S\$..... [2]

- (ii) Calculate the percentage increase in Ben's actual expenditure compared to his projected monthly expenses, correcting your answer to 3 significant figures.

Answer% [2]

[Turn over

7 A local restaurant has 3 outlets in Bishan, Clementi and Orchard Road.

Each outlet offers 4 different set meals at the following prices.

Set A	Set B	Set C	Set D
\$10	\$12	\$14	\$20

The table below shows the number of set meals sold at the different outlets for the month of January.

Set / Outlet	Bishan	Clementi	Orchard Road
Set A	250	100	300
Set B	100	80	150
Set C	50	30	120
Set D	80	20	100

(a) Represent the information given in two matrices, a 1×4 matrix, **P**, and a 4×3 matrix, **Q**.

Answer **P** = [1]

Q = [1]

(b) Evaluate **PQ**.

Answer **PQ** = [2]

(c) Explain what each element in **PQ** represents.

Answer

.....

.....[1]

In view of the Circuit Breaker which took place in the month of April, the restaurant started a delivery service in place of dine-in and offered the different set meals at the same price.

In the month of April, there was a 20% increase for each type of set meal sold at the outlet in Bishan and a decrease of 40% for each type of set meal sold at the outlet in Orchard Road. The number for each type of set meal sold at the Clementi outlet remained the same in the month of April.

The matrix **R**, a 3×1 matrix, is such **PQR** gives the total amount of money collected by the three outlets in the month of April.

(d) Write down matrix **R**.

Answer R = [1]

(e) Evaluate **PQR**.

Answer PQR = [2]

(f) Calculate the difference in the total amount of money collected by the restaurant in April compared to January.


Was there an increase or decrease in the total amount of money collected by the restaurant in April compared to January?

Answer
 [2]


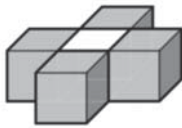
[Turn over

8 A tower is made of grey and white cubes.


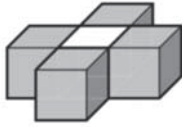
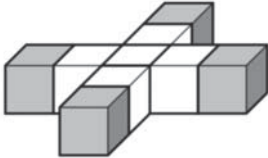
The first layer of the tower is made with one grey cube.

Layer 1	
---------	---

A tower with two layers is made with five grey cubes and one white cube as shown below.

Layer 1	
Layer 2	

A tower with three layers is made with nine grey cubes and six white cubes as shown below.

Layer 1	
Layer 2	
Layer 3	

(a) Complete the table below.

[3]

Number of layers	1	2	3	4	5
Total number of white cubes	0	1	6		
Total number of grey cubes	1	5	9		
Total number of cubes	1	6	15		

(b) Find, in terms of n , the total number of **grey** cubes in a tower with n layers.

Answer [1]

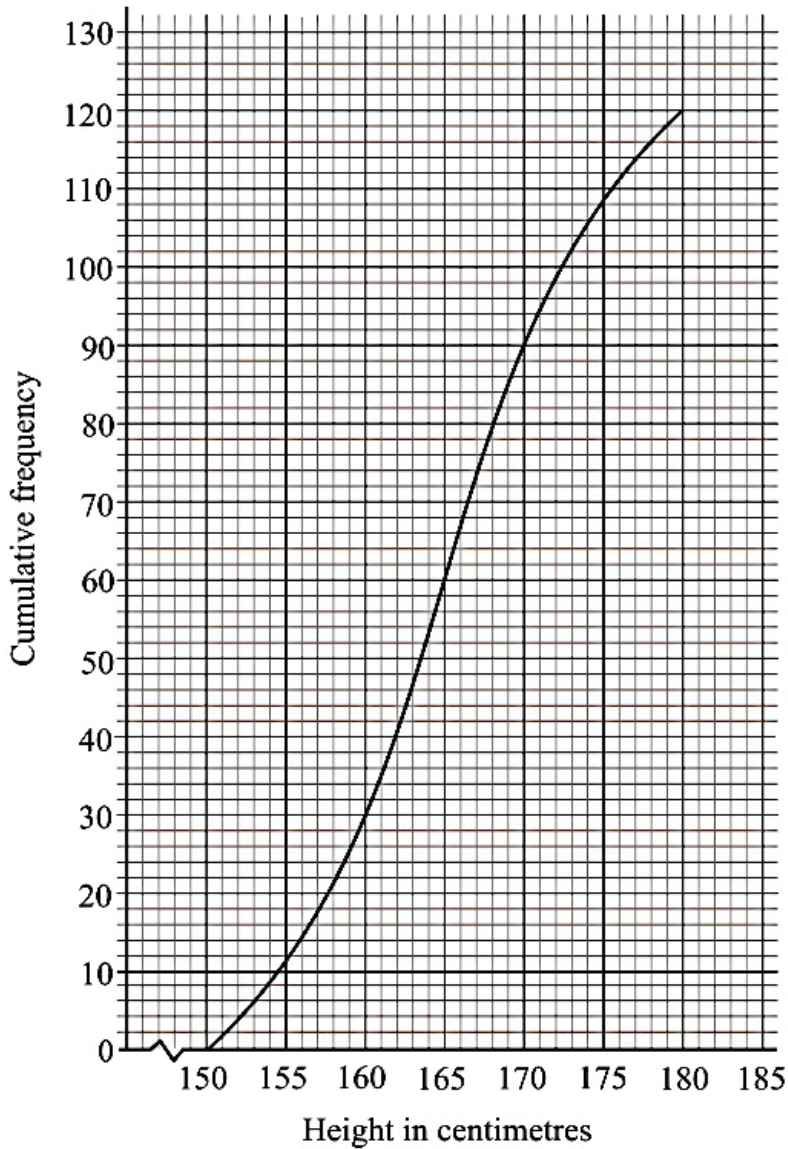
(c) Find, in terms of n , the total number of cubes in a tower with n layers.

Answer [1]

(d) Sarah used 97 grey cubes to build a tower.
Calculate the number of white cubes she used.

Answer cubes [3]

9 The graph below shows the heights of 120 Secondary Four students in a school.



- (a) Using the graph,
 (i) write down the median,

Answer cm [1]

- (ii) find the interquartile range

Answer cm [1]

- (b) Given that 40% of the students are taller than x cm, find the value of x .

Answer $x =$ [1]

[Turn over

- (c) The minimum height requirement to join the school’s basketball team is 175 cm. If two students are randomly selected, calculate the probability that they meet the height requirement for the school’s basketball team.

Answer [2]

- (d) (i) Complete the frequency table below. [2]

Height (cm)	Frequency
$150 < x \leq 155$	
$155 < x \leq 160$	
$160 < x \leq 165$	
$165 < x \leq 170$	
$170 < x \leq 175$	
$175 < x \leq 180$	

- (ii) Estimate the mean height of the students.

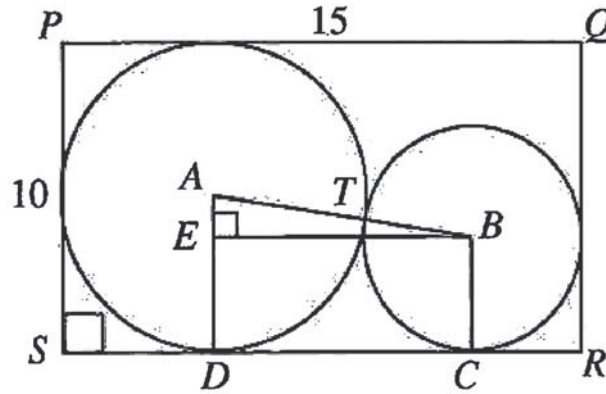
Answercm [1]

- (iii) Estimate the standard deviation of the height of students.

Answercm [1]

10 The diagram shows a rectangle $PQRS$, where $PQ = 15$ cm and $PS = 10$ cm.

The large circle has a centre A and touches three sides of the rectangle.
 The small circle has a centre B and touches two sides of the rectangle.
 The small circle touches the large circle at point T .
 The large and small circles touch the side SR at D and C respectively.
 The point E is the foot of the perpendicular from B to AD .



It is given that the radius of the large circle is 5 cm and the radius of the small circle is x cm.

(a) Write down, in terms of x , an expression for the lengths of
 (i) AB ,

Answer [1]

(ii) AE and

Answer [1]

(iii) DC .

Answer [1]

[Turn over

- (b) Form an equation in x and show that it simplifies to $x^2 - 40x + 100 = 0$. [3]

- (c) Solve $x^2 - 40x + 100 = 0$, giving your answer correct to 2 decimal places.

Answer $x = \dots\dots\dots$ or $x = \dots\dots\dots$ [3]

- (d) Hence, find the radius of the small circle, correct to two decimal places.

Answer $\dots\dots\dots$ cm [1]

[Turn over

- 11 The variables x and y are connected by the equation $y = 2x + \frac{4}{x^2} - 5$.

Some corresponding values of x and y , correct to 2 decimal places, are given in the table below.

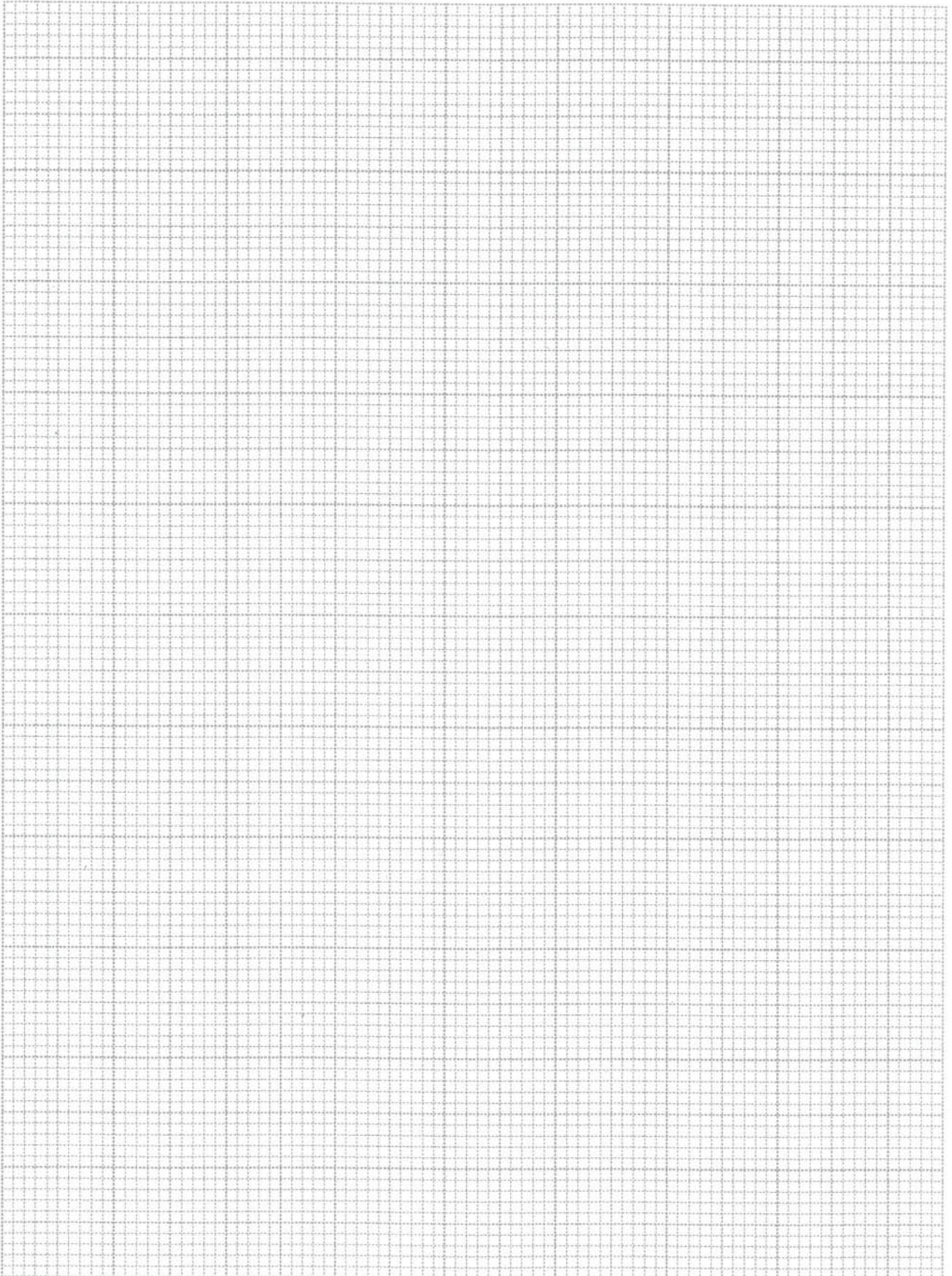
x	0.75	1	1.5	2	3	4	5	6
y	3.61	1	p	0	1.44	3.25	5.16	7.11

- (a) Find the value of p , giving your answer to 2 decimal places.

Answer $p = \dots\dots\dots$ [1]

[Turn over

- (b) Using a scale of 2 cm to represent 1 unit, draw a horizontal x -axis for $0 \leq x \leq 7$.
Using a scale of 2 cm to represent 1 unit, draw a vertical y -axis for $-1 \leq y \leq 8$.
On your axes, plot the points given in the table and join them with a smooth curve. [3]



(c) Use your graph to find,

(i) the least value of y ,

Answer $y = \dots\dots\dots$ [1]

(ii) the range of values of x for which y is less than 2,

Answer $\dots\dots\dots$ [2]

(iii) the solutions of the equation $3x^3 = 14x^2 - 8$ by drawing a suitable straight line.

Answer $x = \dots\dots\dots$ [4]

[Turn over

- 12 The most popular ride at the Outer Space amusement park is the Ferris wheel. The diagram below shows a model of the Ferris wheel at the park.



Each day, the Ferris wheel rides run from 10:30 a.m. to 8:30 p.m. with an hour break for maintenance work at 3 p.m.

The Ferris wheel has 16 passenger cabins. There are seats for 3 passengers in each cabin. Due to recent rules on social distancing, it is mandatory to have an empty seat in between two passengers in each cabin.

Before each ride, passengers take about 5 minutes to be seated and undergo safety checks. At the end of each ride, passengers take about 2 minutes to disembark.

The table below shows the ticket prices for one ride on the Ferris wheel for weekdays and weekends. Tickets must be used on the same day of purchase.

Weekday Ticket	\$18
Weekend Ticket	\$23

- (a) Given that the Ferris wheel makes 1 revolution every two minutes and makes 4 revolutions per ride, calculate the total number of rides each cabin on the Ferris wheel makes in one day.

Answerrides [2]

- (b) Calculate the maximum number of passengers that the Ferris wheel can take in one day.

Answerpassengers [1]

[Turn over

- (c) If all the seats are taken up for every ride, calculate the total amount of money that the park can collect from the sale of tickets for Ferris wheel rides on a weekday.

Answer \$..... [1]

- (d) To commemorate its tenth birthday, the amusement park is planning to give out free tickets for its Ferris wheel rides.

Propose a sensible number of tickets to be given free such that the amount collected from the sale of tickets sales for the day covers its operating cost of \$10 000. It is also estimated that 40% to 60% of the total possible seats will be taken for each ride.

Explain your proposal clearly and state any assumptions made.

(d)

Answer
.....
.....
.....[6]

End of Paper

[Turn over

